1. **(3 points)** Let $X_1, ..., X_n$ be a random sample from $N(\mu, \sigma^2)$ distribution.

   Show that $\bar{X} = \frac{1}{n}\sum_{i=1}^{n} X_i$ has $N\left(\mu, \frac{\sigma^2}{n}\right)$ distribution.