1. Let $f : [a, b] \to \mathbb{R}$ be a bounded function. Prove that f is integrable iff for every $\varepsilon > 0$, there exists a partition P such that $\mathcal{U}_P(f) - \mathcal{L}_P(f) < \varepsilon$.